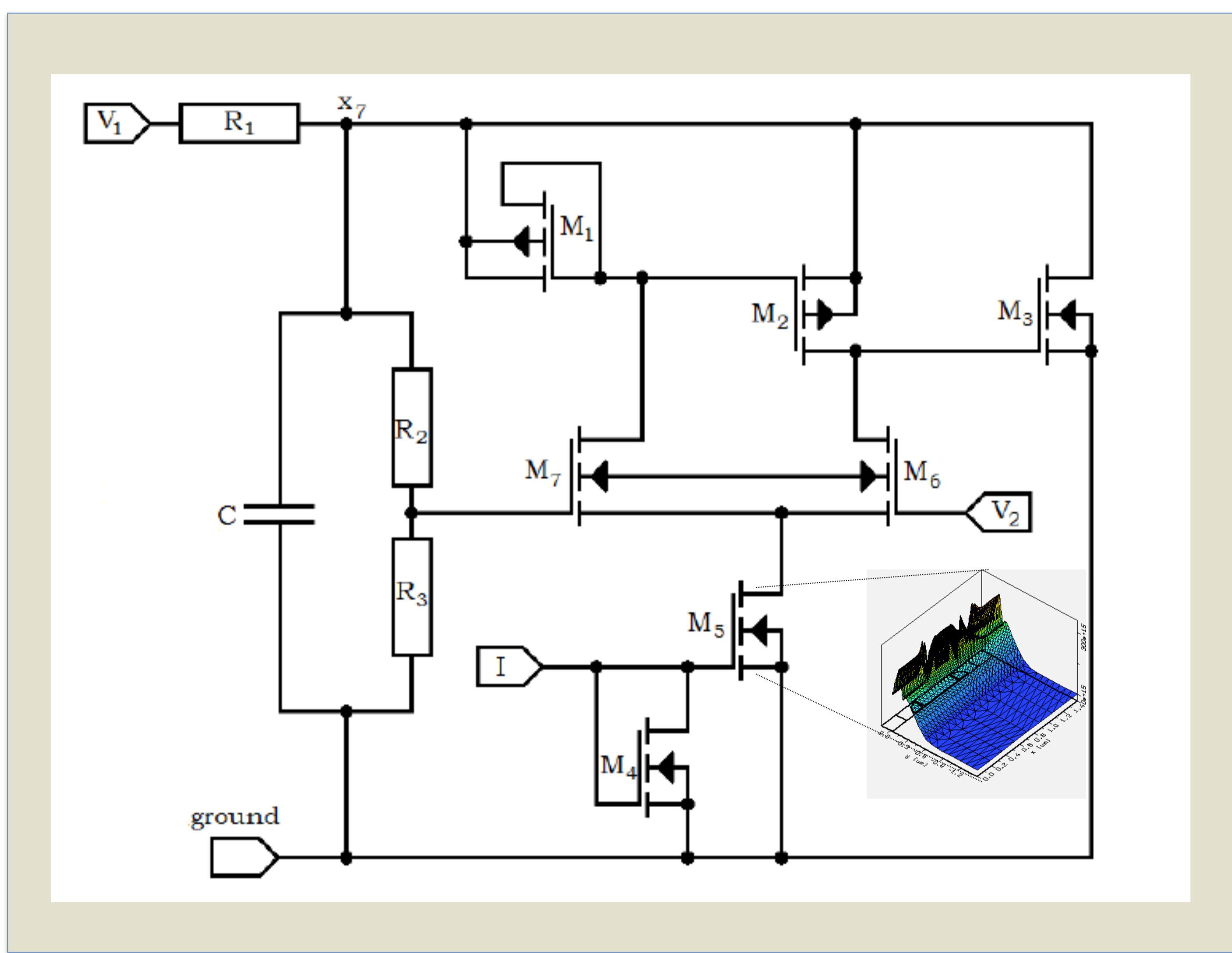


## Fully Coupled Circuit and Device Simulation with Exploitation of Algebraic Multigrid Linear Solver

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### WHAT WE ARE DOING

We solve coupled systems of differential-algebraic equations (DAEs) and partial differential equations (PDAEs). With MECS we implemented a combined circuit/device simulation framework with a calling interface to Minimos-NT.



Circuit with one device fully discretized and all others computed by compact models

### AVOIDING ZERO ENTRIES ON THE DIAGONAL

#### Problem:

MNA generates zero entries on the diagonal of the Jacobian. Zero diagonal should be avoided for algebraic multigrid method.

#### Approach:

Origin of non-zeros are: voltage sources and inductivities. Voltage source equations can be eliminated by substitution. Inductivity equations can be equivalently transformed:

$$\begin{array}{ccc|ccc}
 0 & & & & & 1 \\
 & & & & & \dots \\
 & & & & & -1 \\
 & & & & & \dots \\
 -1 & & & 1 & & L\alpha_0/h
 \end{array}
 \Rightarrow
 \begin{array}{ccc|ccc}
 h/(L\alpha_0) & -h/(L\alpha_0) & & & & 0 \\
 & & & & & \dots \\
 -h/(L\alpha_0) & h/(L\alpha_0) & & & & 0 \\
 & & & & & \dots \\
 -1 & & & 1 & & L\alpha_0/h
 \end{array}$$

Modified Nodal Approach (MNA)

Jacobian part after transformation

#### Result:

MNA matrices can be transformed to non-zero diagonal form which is much more suitable for algebraic multigrid linear solver.

### FIELDS OF APPLICATION

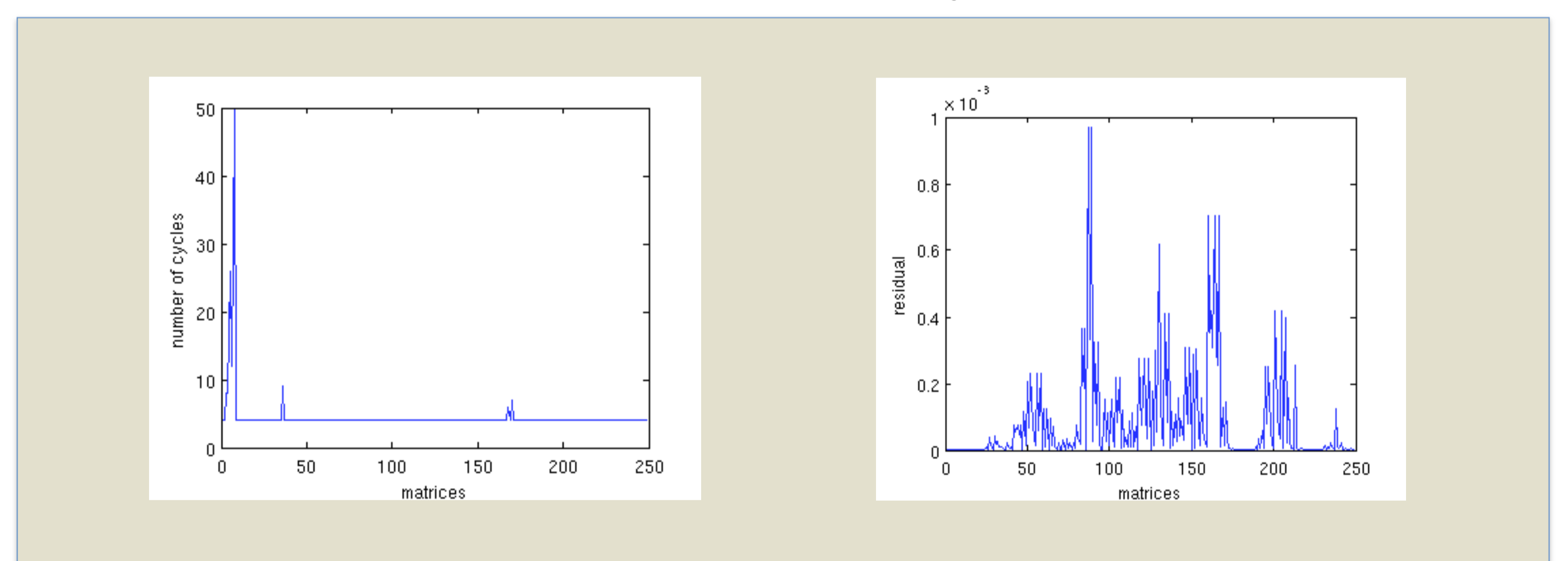
- Fully coupled electrical and device simulation
- Integration of Spice3 (BSIM) for compact transistor models
- Integration of Minimos-NT for the device parts
- Integration of field solver Magwel for electromagnetic devices
- Special variants for simulation of water or gas networks
- Sensitivity analysis of parameter variations (DesParO)



Graphical user's interface of DesParO explorer

### RESULTS

First tests with SAMG solver with two fully discretized devices:



Cycle numbers (left) and residuals after convergence (right) for algebraic multigrid solver (SAMG)

### CONCLUSION

Algebraic multigrid solvers can be successfully applied to coupled circuit/device simulation. Larger problems will considerably benefit since computational complexity is linear.

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