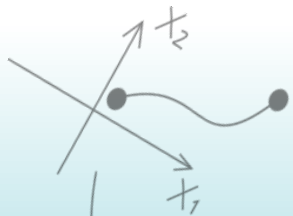


Structural Error Estimation in Dynamic Systems

Dominik Kahl, Philipp Wendlandt
 Andreas Weber, Maik Kschischo

18.09.2018



Handwritten mathematical notes and diagrams:

- Equation: $G^* G_{ij} = \sum_{n,m=0}^{\infty} \sum_{t \in T} \sum_{\tau \in T} F(\tau \oplus \varphi) \varphi \in \Gamma_m(s, t)$
- Equation: $\int_0^{\tau-t} \frac{(\tau-t)^m (t-s)^n}{m! n!} \varphi(s) ds dt$
- Graph: A plot of $\|G^* G\|$ vs τ showing two curves (red and green) that increase and then level off.
- Text: "früher" (earlier) written vertically on the right side.
- Text: $\ker g = \phi$ written near the top right.

Gefördert durch

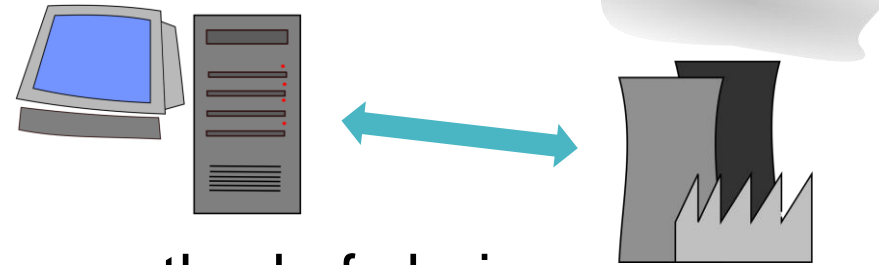


- SEEDS is supported by Deutsche Forschungsgesellschaft
Project - Nr. 354645666
- SEEDS contains a PhD-Project in cooperation with University Bonn

Supervised by Andreas Weber (Bonn)
 and Maik Kschischo (Koblenz)

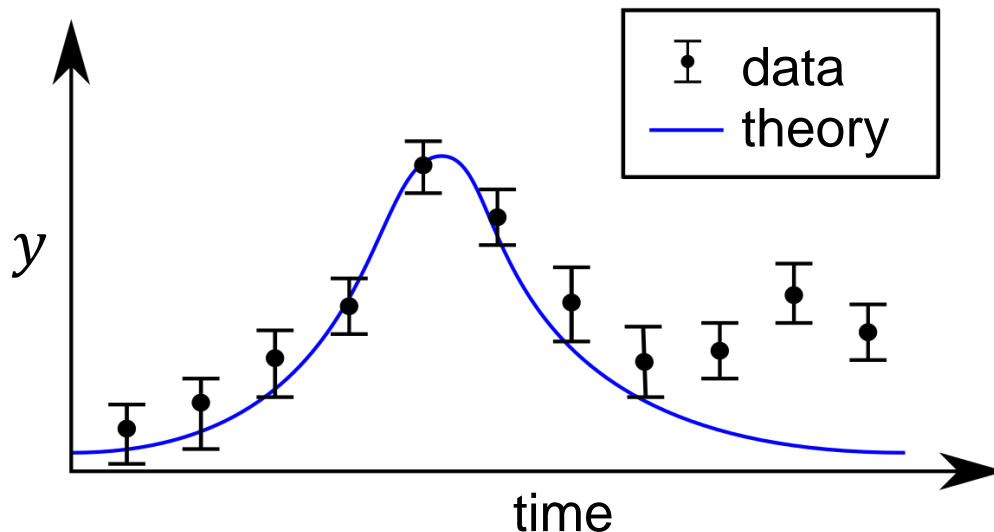
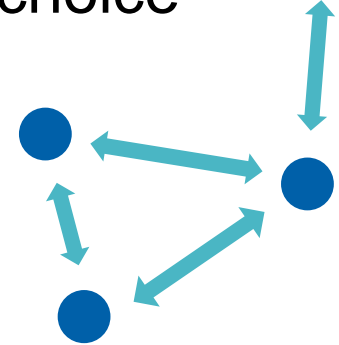
Dynamic Systems

Biology, Pharmacy, Physics ...



Dynamic Systems are the method of choice

$$\begin{cases} \dot{x} = f(x, u) & (\text{Dynamic Equation}) \\ y = h(x) & (\text{Observation}) \end{cases}$$



Experts are needed to improve the model

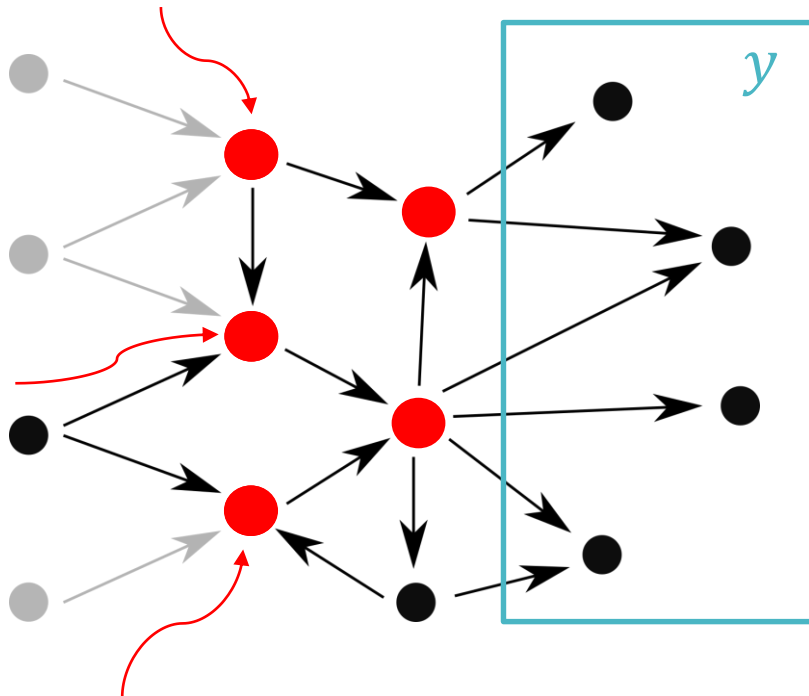
Models can reach
100 - 1000 dimensions

Criteria

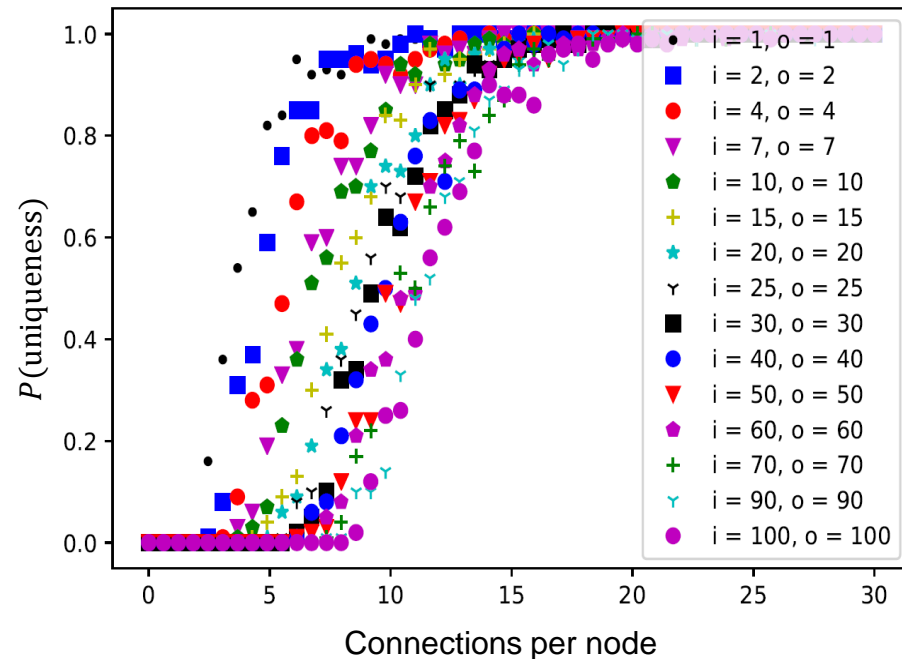
Is it possible to identify the model error?



Analytical and graphical criteria
running in polynomial time

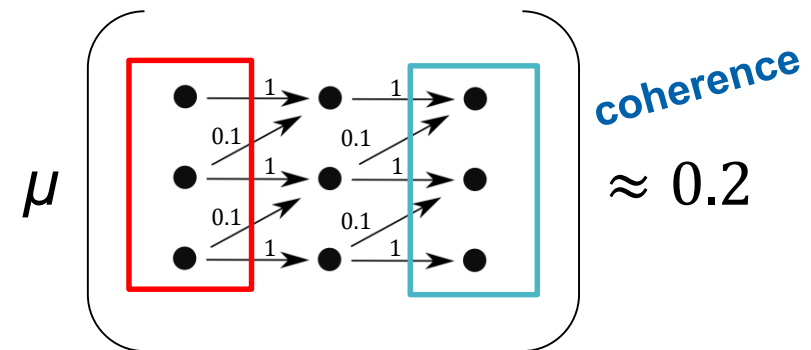
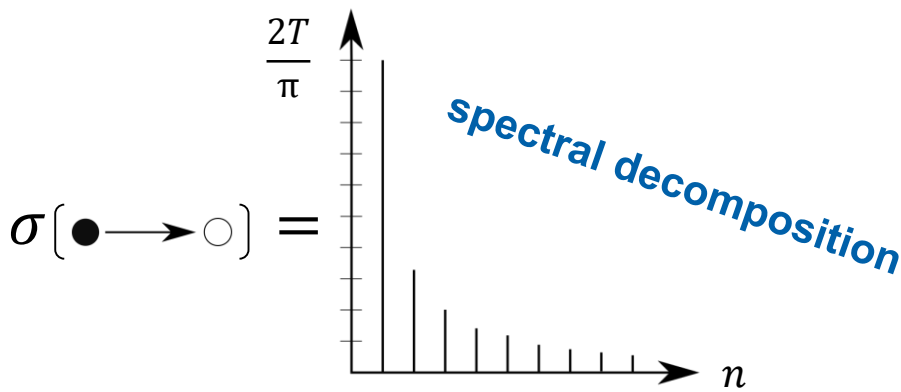
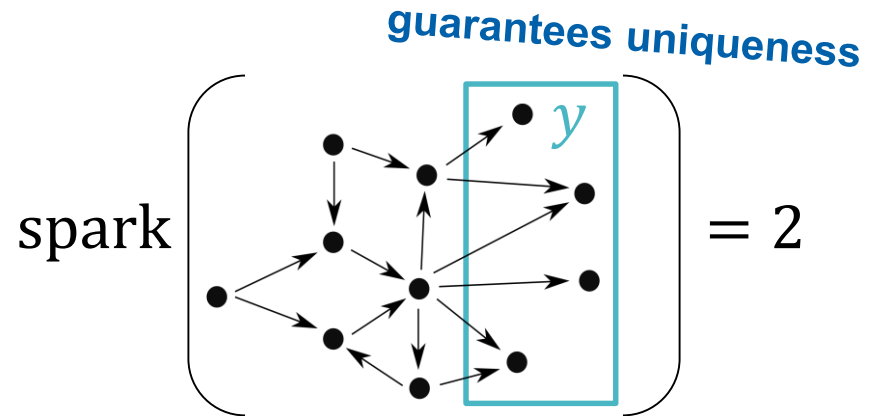


Phase transition in homogeneous networks



Compressed Error Sensing

Static Compressed Sensing
led to remarkable results.
We extend it to dynamic
systems ...

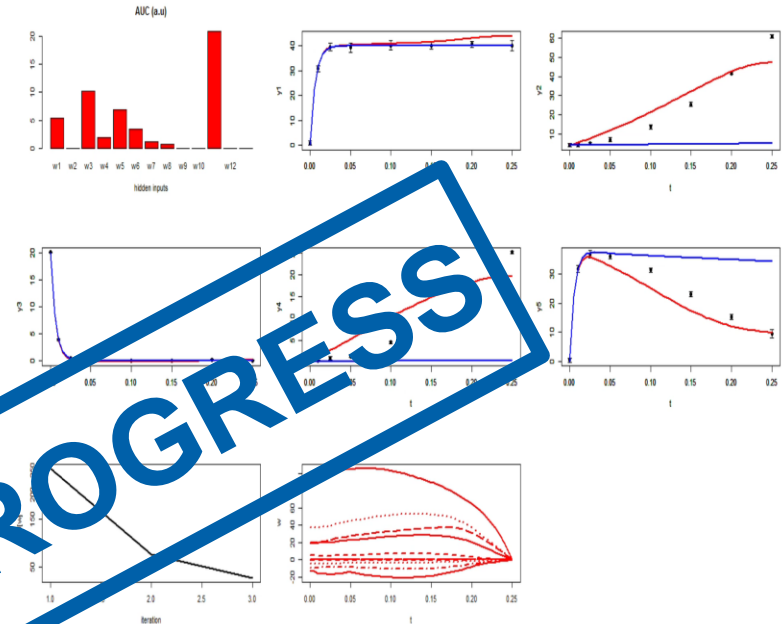


Future Prospects

Dynamic Elastic Net [1]



Optimization procedure
to find model errors



Bio - Networks



Did evolution optimize
network topology?

Theory of dynamic compressed sensing



Sensor placement
Experimental Design

SEEDS

Structural Error Estimation in Dynamic Systems

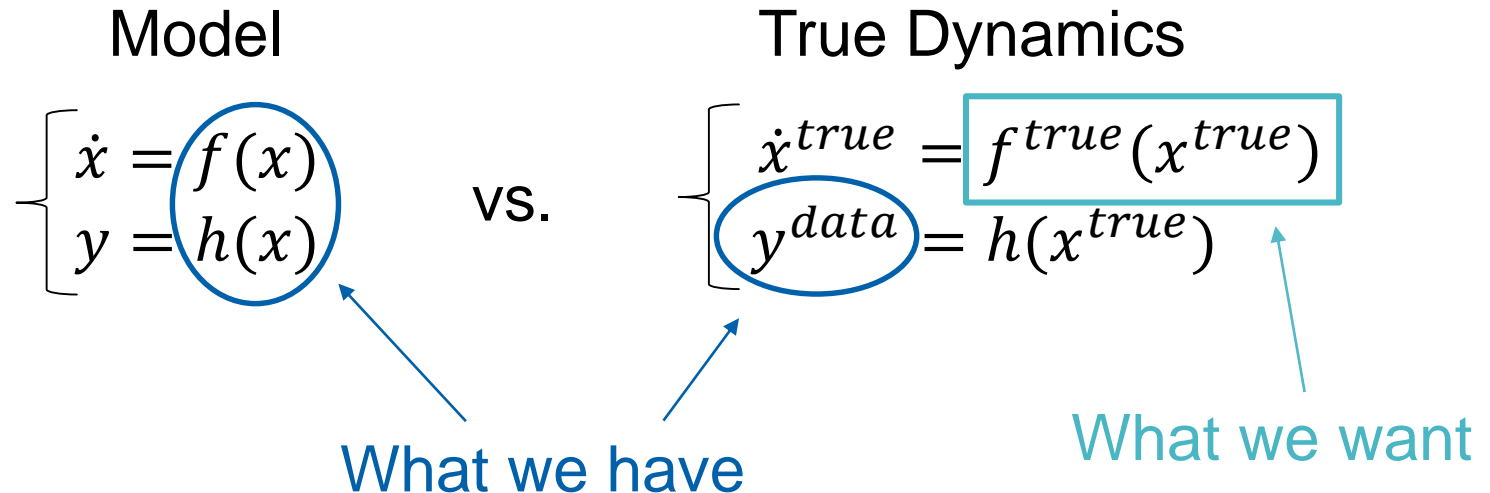
Thank you for your attention

Literature

- [1] Benjamin Engelhardt, Holger Fröhlich, and Maik Kschischo. *Learning (from) the errors of a systems biology model*. Scientific Reports, 6, November 2016.

Structural Error

Estimation



Correct the model with a hidden input w

$$\dot{\hat{x}} = f(\hat{x}) + w \quad \text{to get} \quad y^{data} = h(\hat{x})$$



Does w exist and is it unique?